



Exercise: 08

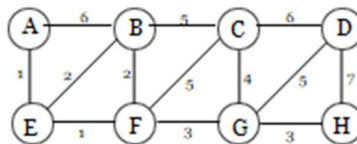
GRAPHS AND SPANNING TREE

18 - Oct - 2024

Spot (5 Marks)

1.

Consider the following graph



- ▮ What is the cost of its minimum spanning tree?
 - ▮ How many minimum spanning trees does it have?
 - ▮ Suppose Kruskal's algorithm is run on this graph. In what order are the edges added to the MST? For each edge in this sequence, give a cut that justifies its addition
2. Implement prim's algorithm for the above graph.

Consider an undirected graph $G = (V, E)$ with nonnegative edge weights $w_e \geq 0$. Suppose that you have computed a minimum spanning tree of G .

Now suppose each edge weight is increased by 1: the new weights are $w_e' = w_e + 1$.

- ▮ Does the minimum spanning tree change? Give an example where it changes or prove it cannot change